

Linear Inequalities

Question 1.

If $-2 < 2x - 1 < 2$ then the value of x lies in the interval

- (a) $(1/2, 3/2)$
- (b) $(-1/2, 3/2)$
- (c) $(3/2, 1/2)$
- (d) $(3/2, -1/2)$

Answer: (b) $(-1/2, 3/2)$

Given, $-2 < 2x - 1 < 2$

$$\Rightarrow -2 + 1 < 2x < 2 + 1$$

$$\Rightarrow -1 < 2x < 3$$

$$\Rightarrow -1/2 < x < 3/2$$

$$\Rightarrow x \in (-1/2, 3/2)$$

Question 2.

If $x^2 < -4$ then the value of x is

- (a) $(-2, 2)$
- (b) $(2, \infty)$
- (c) $(-2, \infty)$
- (d) No solution

Answer: (d) No solution

Given, $x^2 < -4$

$$\Rightarrow x^2 + 4 < 0$$

Which is not possible.

So, there is no solution.

Question 3.

If $|x| < -5$ then the value of x lies in the interval

- (a) $(-\infty, -5)$
- (b) $(\infty, 5)$

- (c) $(-5, \infty)$
(d) No Solution

Answer: (d) No Solution

Given, $|x| < -5$

Now, $LHS \geq 0$ and $RHS < 0$

Since LHS is non-negative and RHS is negative

So, $|x| < -5$ does not possess any solution

Question 4.

The graph of the inequations $x \leq 0$, $y \leq 0$, and $2x + y + 6 \geq 0$ is

- (a) exterior of a triangle
(b) a triangular region in the 3rd quadrant
(c) in the 1st quadrant
(d) none of these

Answer: (b) a triangular region in the 3rd quadrant

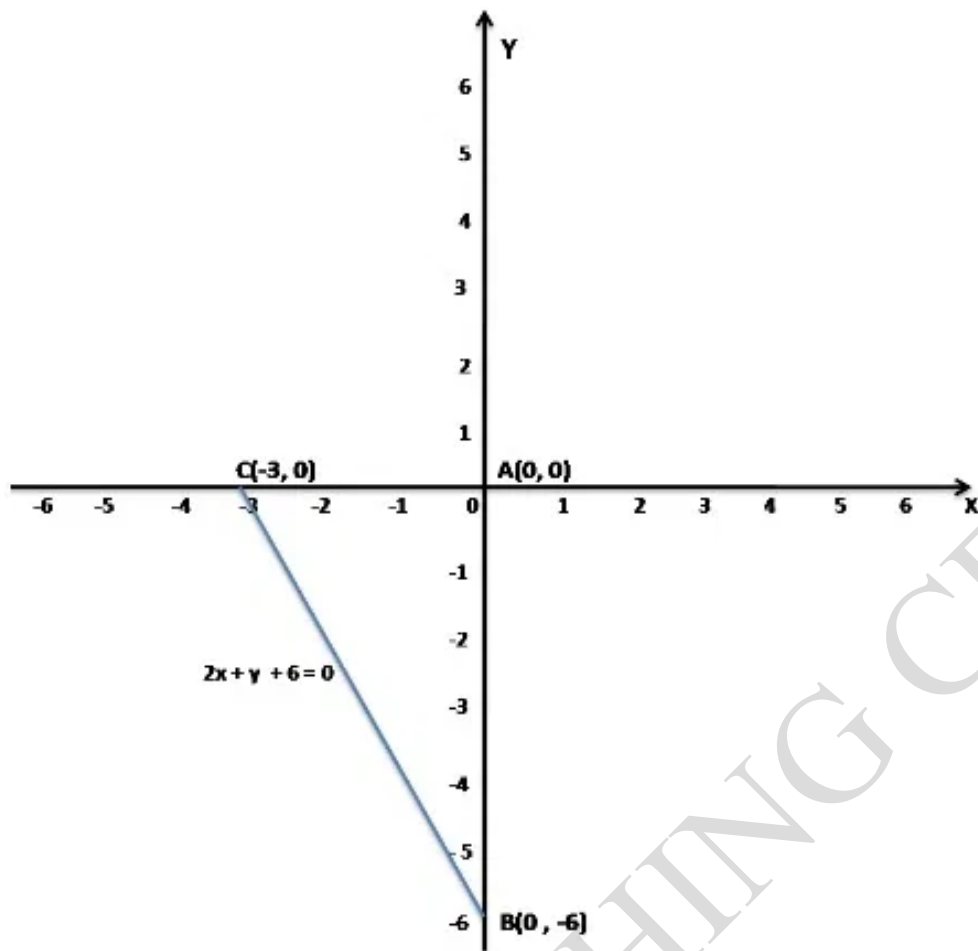
Given inequalities $x \geq 0$, $y \geq 0$, $2x + y + 6 \geq 0$

Now take $x = 0$, $y = 0$ and $2x + y + 6 = 0$

when $x = 0$, $y = -6$

when $y = 0$, $x = -3$

So, the points are $A(0, 0)$, $B(0, -6)$ and $C(-3, 0)$



So, the graph of the inequations $x \leq 0$, $y \leq 0$, and $2x + y + 6 \geq 0$ is a triangular region in the 3rd quadrant.

Question 5.

The graph of the inequalities $x \geq 0$, $y \geq 0$, $2x + y + 6 \leq 0$ is

- (a) a square
- (b) a triangle
- (c) $\{ \}$
- (d) none of these

Answer: (c) $\{ \}$

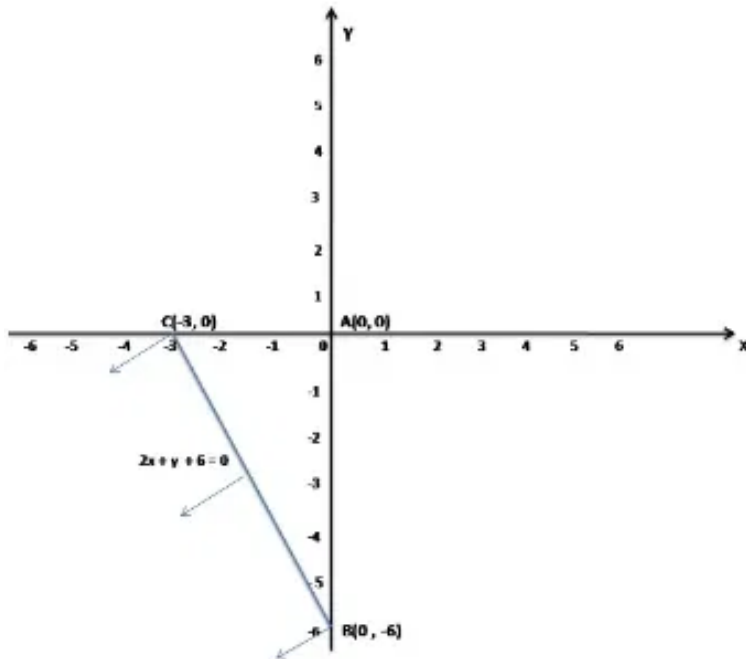
Given inequalities $x \geq 0$, $y \geq 0$, $2x + y + 6 \leq 0$

Now take $x = 0$, $y = 0$ and $2x + y + 6 = 0$

when $x = 0$, $y = -6$

when $y = 0$, $x = -3$

So, the points are $A(0, 0)$, $B(0, -6)$ and $C(-3, 0)$



Since region is outside from the line $2x + y + 6 = 0$
So, it does not represent any figure.

Question 6.

Solve: $2x + 1 > 3$

- (a) $[-1, \infty]$
- (b) $(1, \infty)$
- (c) (∞, ∞)
- (d) $(\infty, 1)$

Answer: (b) $(1, \infty)$

Given, $2x + 1 > 3$

$$\Rightarrow 2x > 3 - 1$$

$$\Rightarrow 2x > 2$$

$$\Rightarrow x > 1$$

$$\Rightarrow x \in (1, \infty)$$

Question 7.

The solution of the inequality $3(x - 2)/5 \geq 5(2 - x)/3$ is

- (a) $x \in (2, \infty)$
- (b) $x \in [-2, \infty)$
- (c) $x \in [\infty, 2)$
- (d) $x \in [2, \infty)$

Answer: (d) $x \in [2, \infty)$

Given, $3(x - 2)/5 \geq 5(2 - x)/3$

$$\Rightarrow 3(x - 2) \times 3 \geq 5(2 - x) \times 5$$

$$\Rightarrow 9(x - 2) \geq 25(2 - x)$$

$$\Rightarrow 9x - 18 \geq 50 - 25x$$

$$\Rightarrow 9x - 18 + 25x \geq 50$$

$$\Rightarrow 34x - 18 \geq 50$$

$$\Rightarrow 34x \geq 50 + 18$$

$$\Rightarrow 34x \geq 68$$

$$\Rightarrow x \geq 68/34$$

$$\Rightarrow x \geq 2$$

$$\Rightarrow x \in [2, \infty)$$

Question 8.

Solve: $1 \leq |x - 1| \leq 3$

(a) $[-2, 0]$

(b) $[2, 4]$

(c) $[-2, 0] \cup [2, 4]$

(d) None of these

Answer: (c) $[-2, 0] \cup [2, 4]$

Given, $1 \leq |x - 1| \leq 3$

$$\Rightarrow -3 \leq (x - 1) \leq -1 \text{ or } 1 \leq (x - 1) \leq 3$$

i.e. the distance covered is between 1 unit to 3 units

$$\Rightarrow -2 \leq x \leq 0 \text{ or } 2 \leq x \leq 4$$

Hence, the solution set of the given inequality is

$$x \in [-2, 0] \cup [2, 4]$$

Question 9.

Solve: $-1/(|x| - 2) \geq 1$ where $x \in \mathbb{R}$, $x \neq \pm 2$

(a) $(-2, -1)$

(b) $(-2, 2)$

(c) $(-2, -1) \cup (1, 2)$

(d) None of these

Answer: (c) $(-2, -1) \cup (1, 2)$

Given, $-1/(|x| - 2) \geq 1$

$$\Rightarrow -1/(|x| - 2) - 1 \geq 0$$

$$\Rightarrow \{-1 - (|x| - 2)\}/(|x| - 2) \geq 0$$

$$\Rightarrow \{1 - |x|\} / (|x| - 2) \geq 0$$

$$\Rightarrow \frac{-(|x| - 1)}{(|x| - 2)} \geq 0$$

$$\frac{1}{-} \quad \frac{2}{+} \quad \frac{-}{-}$$

Using number line rule:

$$1 \leq |x| < 2$$

$$\Rightarrow x \in (-2, -1) \cup (1, 2)$$

Question 10.

If $x^2 < 4$ then the value of x is

- (a) (0, 2)
- (b) (-2, 2)
- (c) (-2, 0)
- (d) None of these

Answer: (b) (-2, 2)

Given, $x^2 < 4$

$$\Rightarrow x^2 - 4 < 0$$

$$\Rightarrow (x - 2) \times (x + 2) < 0$$

$$\Rightarrow -2 < x < 2$$

$$\Rightarrow x \in (-2, 2)$$

Question 11.

Solve: $2x + 1 > 3$

- (a) [1, 1)
- (b) (1, ∞)
- (c) (∞ , ∞)
- (d) (∞ , 1)

Answer: (b) (1, ∞)

Given, $2x + 1 > 3$

$$\Rightarrow 2x > 3 - 1$$

$$\Rightarrow 2x > 2$$

$$\Rightarrow x > 1$$

$$\Rightarrow x \in (1, \infty)$$

Question 12.

If a is an irrational number which is divisible by b then the number b

- (a) must be rational
- (b) must be irrational
- (c) may be rational or irrational
- (d) None of these

Answer: (b) must be irrational

If a is an irrational number which is divisible by b then the number b must be irrational.

Ex: Let the two irrational numbers are $\sqrt{2}$ and $\sqrt{3}$

Now, $\sqrt{2}/\sqrt{3} = \sqrt{2/3}$

Question 13.

Sum of two rational numbers is _____ number.

- (a) rational
- (b) irrational
- (c) Integer

Answer: (a) rational

The sum of two rational numbers is a rational number.

Ex: Let two rational numbers are $1/2$ and $1/3$

Now, $1/2 + 1/3 = 5/6$ which is a rational number.

Question 14.

If $|x| = -5$ then the value of x lies in the interval

- (a) $(-5, \infty)$
- (b) $(5, \infty)$
- (c) $(\infty, -5)$
- (d) No solution

Answer: (d) No solution

Given, $|x| = -5$

Since $|x|$ is always positive or zero

So, it can not be negative

Hence, given inequality has no solution.

Question 15.

The value of x for which $|x + 1| + \sqrt{x - 1} = 0$

- (a) 0
- (b) 1

- (c) -1
(d) No value of x

Answer: (d) No value of x

Given, $|x + 1| + \sqrt{x - 1} = 0$, where each term is non-negative.

So, $|x + 1| = 0$ and $\sqrt{x - 1} = 0$ should be zero simultaneously.

i.e. $x = -1$ and $x = 1$, which is not possible.

So, there is no value of x for which each term is zero simultaneously.

Question 16.

If $x^2 < -4$ then the value of x is

- (a) $(-2, 2)$
(b) $(2, \infty)$
(c) $(-2, \infty)$
(d) No solution

Answer: (d) No solution

Given, $x^2 < -4$

$$\Rightarrow x^2 + 4 < 0$$

Which is not possible.

So, there is no solution.

Question 17.

The solution of $|2/(x - 4)| > 1$ where $x \neq 4$ is

- (a) $(2, 6)$
(b) $(2, 4) \cup (4, 6)$
(c) $(2, 4) \cup (4, \infty)$
(d) $(-\infty, 4) \cup (4, 6)$

Answer: (b) $(2, 4) \cup (4, 6)$

Given, $|2/(x - 4)| > 1$

$$\Rightarrow 2/|x - 4| > 1$$

$$\Rightarrow 2 > |x - 4|$$

$$\Rightarrow |x - 4| < 2$$

$$\Rightarrow -2 < x - 4 < 2$$

$$\Rightarrow -2 + 4 < x < 2 + 4$$

$$\Rightarrow 2 < x < 6$$

$$\Rightarrow x \in (2, 6), \text{ where } x \neq 4$$

$$\Rightarrow x \in (2, 4) \cup (4, 6)$$

Question 18.

The solution of the function $f(x) = |x| > 0$ is

- (a) $\mathbb{R}$
- (b) $\mathbb{R} - \{0\}$
- (c) $\mathbb{R} - \{1\}$
- (d) $\mathbb{R} - \{-1\}$

Answer: (b) $\mathbb{R} - \{0\}$

Given, $f(x) = |x| > 0$

We know that modulus is non negative quantity.

So, $x \in \mathbb{R}$ except that $x = 0$

$\Rightarrow x \in \mathbb{R} - \{0\}$

This is the required solution

Question 19.

Solve: $|x - 1| \leq 5, |x| \geq 2$

- (a) $[2, 6]$
- (b) $[-4, -2]$
- (c) $[-4, -2] \cup [2, 6]$
- (d) None of these

Answer: (c) $[-4, -2] \cup [2, 6]$

Given, $|x - 1| \leq 5, |x| \geq 2$

$\Rightarrow -(5 \leq (x - 1) \leq 5), (x \leq -2 \text{ or } x \geq 2)$

$\Rightarrow -(4 \leq x \leq 6), (x \leq -2 \text{ or } x \geq 2)$

Now, required solution is

$x \in [-4, -2] \cup [2, 6]$

Question 20.

The solution of the $15 < 3(x - 2)/5 < 0$ is

- (a) $27 < x < 2$
- (b) $27 < x < -2$
- (c) $-27 < x < 2$
- (d) $-27 < x < -2$

Answer: (a) $27 < x < 2$

Given inequality is:

$15 < 3(x - 2)/5 < 0$

$\Rightarrow 15 \times 5 < 3(x - 2) < 0 \times 5$

$\Rightarrow 75 < 3(x - 2) < 0$

$\Rightarrow 75/3 < x - 2 < 0$

$$\Rightarrow 25 < x - 2 < 0$$

$$\Rightarrow 25 + 2 < x < 0 + 2$$

$$\Rightarrow 27 < x < 2$$

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